

Saturation

$$S_i = \frac{\text{volume of phase } i}{\text{pore volume}} = \frac{V_i}{V_p}$$

1-phase (e.g. water) $S_w = \frac{V_w}{V_p} = \frac{V_p}{V_p} = 1$

2-phase (e.g. water & oil)

$$\frac{V_w}{V_p} + \frac{V_o}{V_p} = \frac{V_p}{V_p}$$

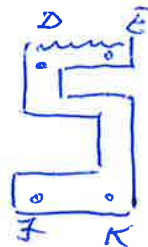
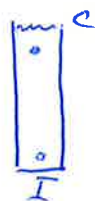
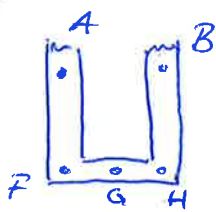
$$S_w + S_o = 1$$

3-phase

$$V_o + V_w + V_g = V_p$$

$$\Rightarrow \underline{S_o + S_w + S_g = 1}$$

Pressure

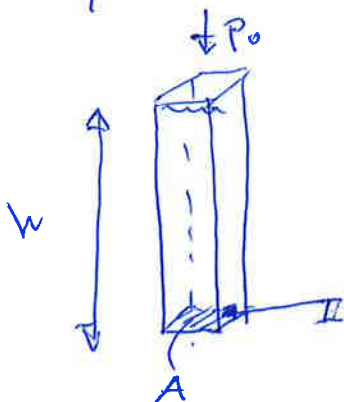


$$P_A = P_B = P_C = P_D = P_E$$

$$P_F = P_G = P_H = P_I = P_J = P_K$$

relation between pressure at point C & I!

pressure = Force / area



force in point I: $F = P_0 \cdot A + m_w \cdot g$

$$m_w = \rho_w \cdot V = \rho_w \cdot A \cdot h$$

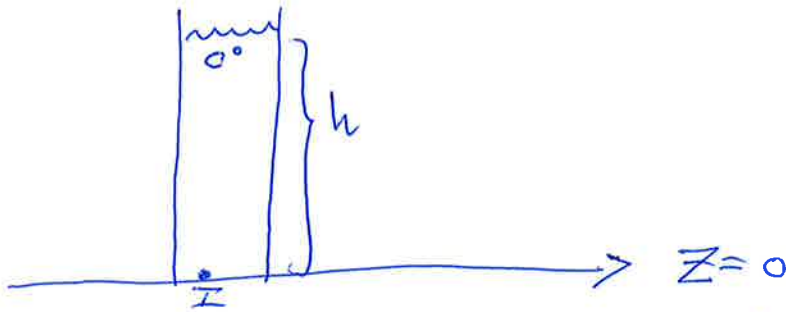
$$\underline{P_I} = \frac{F}{A} = \frac{P_0 \cdot A + \rho_w \cdot g \cdot A \cdot h}{A} = \underline{P_0 + \rho_w \cdot g \cdot h}$$

useful quantity $\psi = p + \rho g z$

$$\left[\bar{\phi} = \frac{\psi}{\rho} = \frac{p}{\rho} + g z \right]$$

z = distance from datum plane

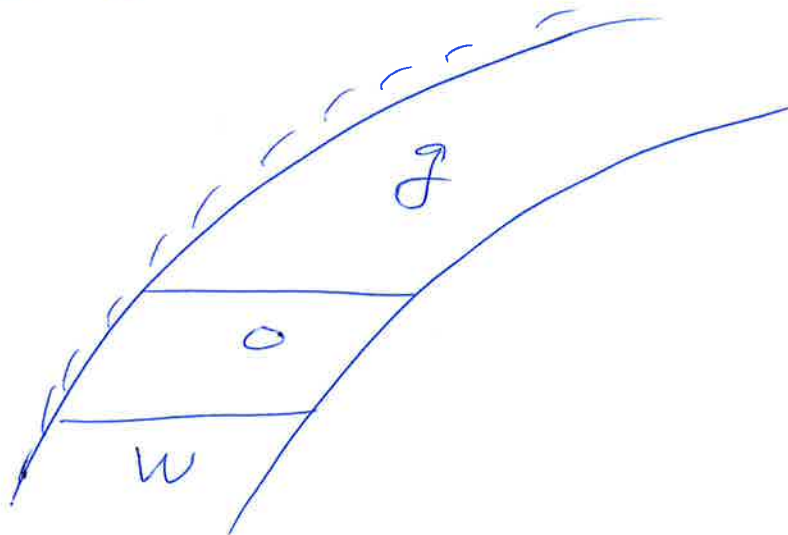
ex:



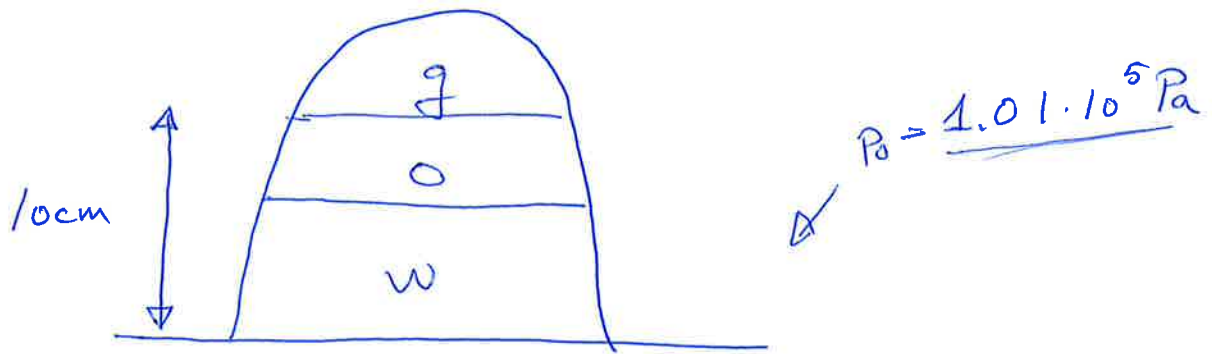
potential in c: $\psi_c = p_c + \rho g \frac{z}{h}$

I: $\psi_I = p_I$

$$p_I = p_c + \rho g h \Rightarrow \psi_I = p_c + \rho g h = \psi_c$$



experiment



$$\rho_w = \rho_o = 1000 \text{ kg/m}^3$$

$$\Delta p = \rho_w g h = 10^3 \cdot 10 \cdot 0.1 \text{ Pa} = 10^3 \text{ Pa}$$

gas phase expands when the glass is turned

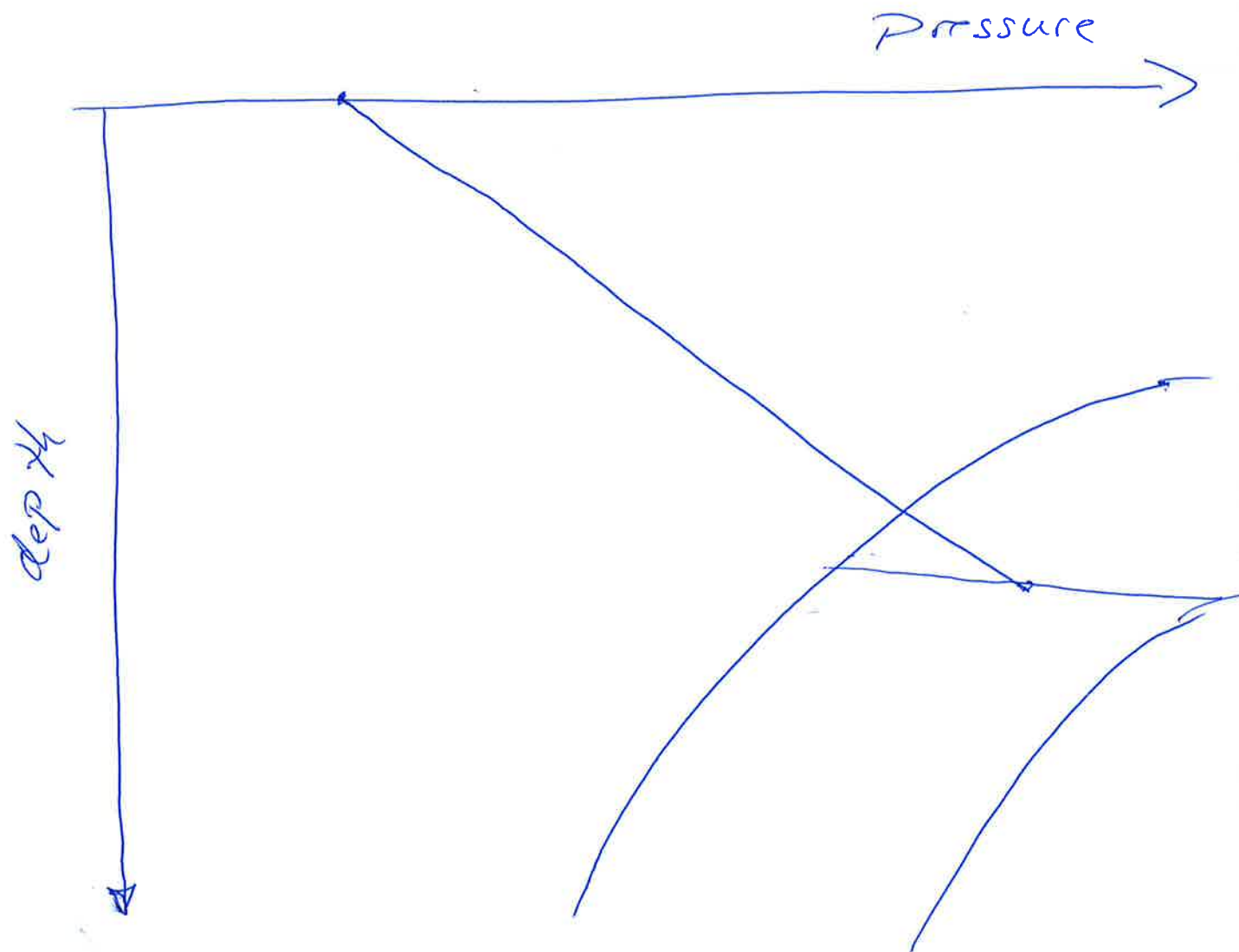
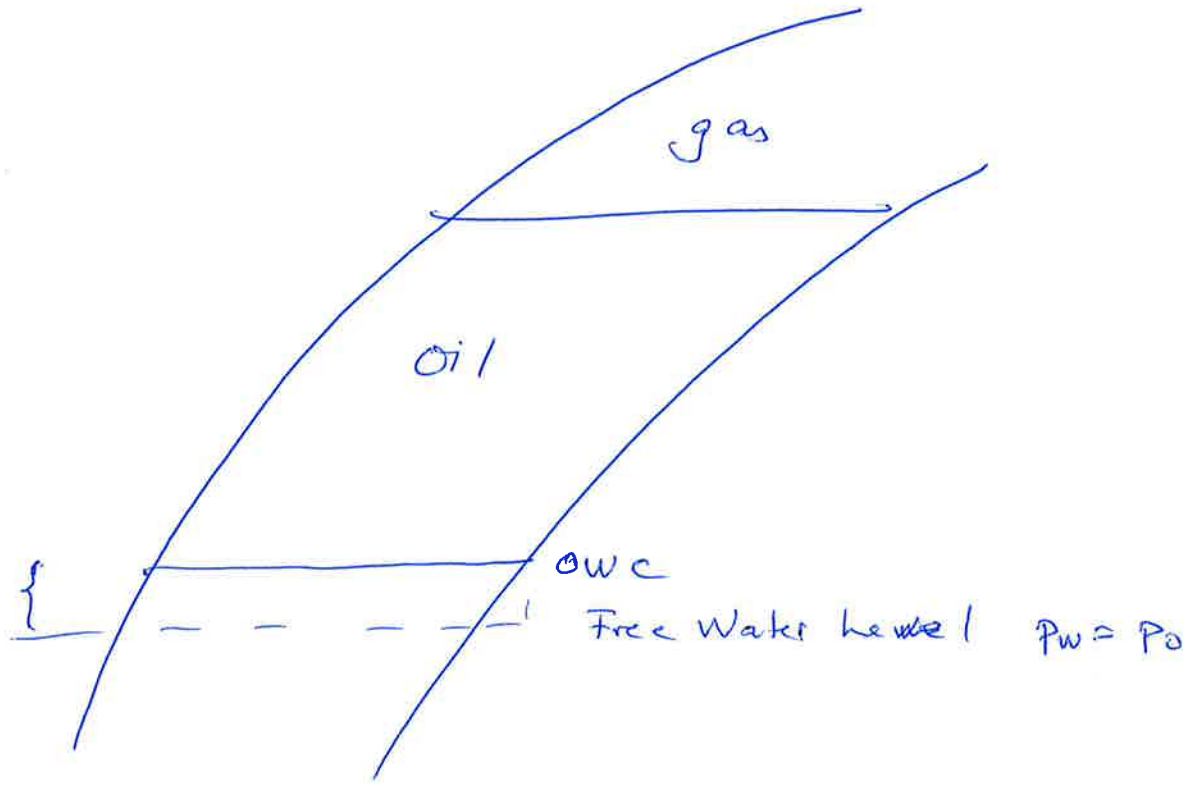
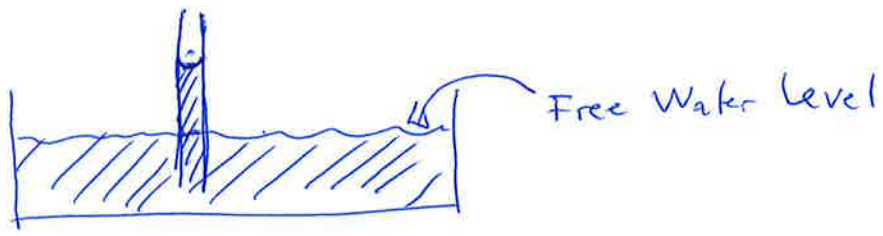
ideal gas

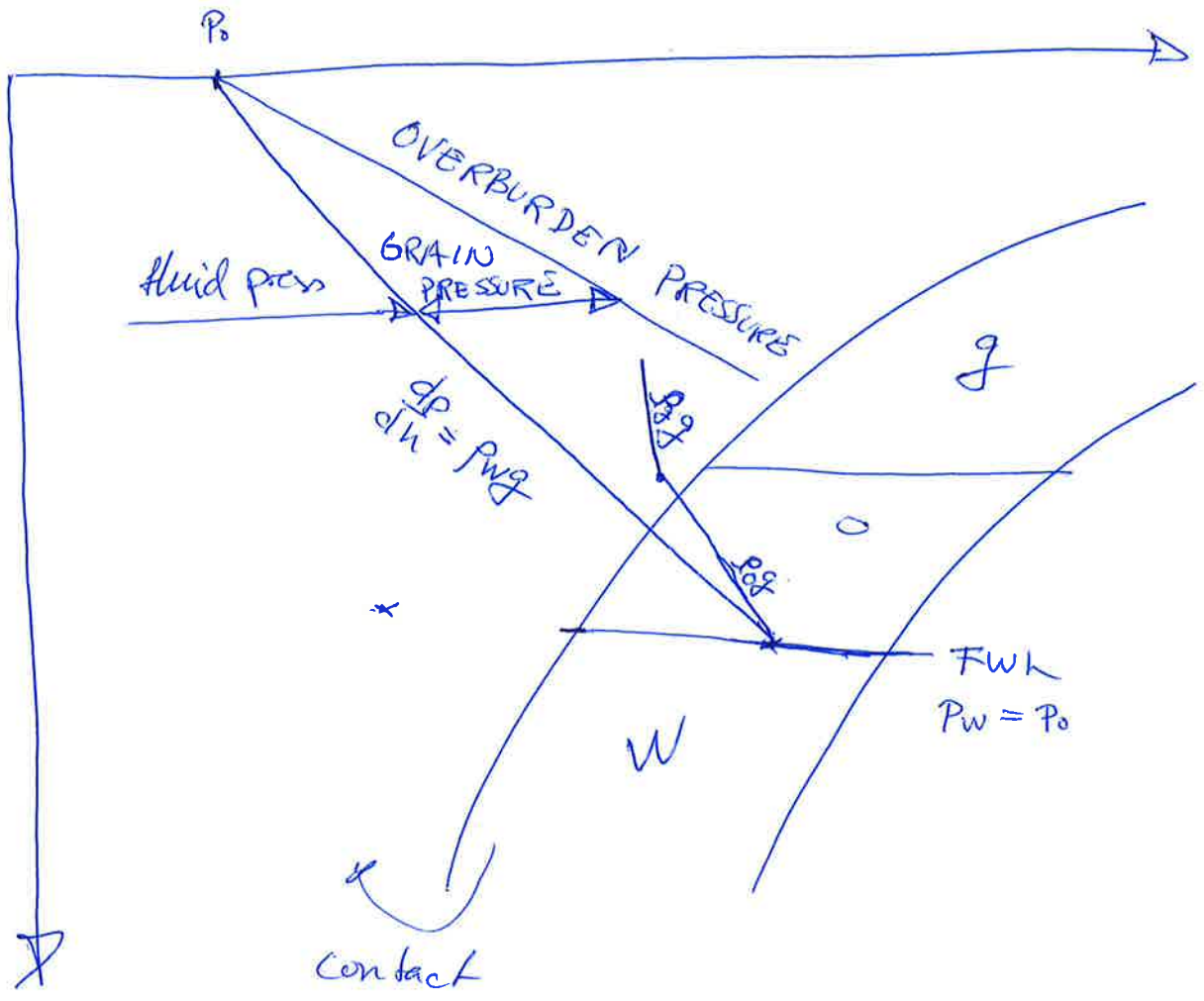
$$P_i V_i = P_f^* V_f$$

$$P_f^* = P_i \frac{V_i}{V_f} = P_i \frac{V_i}{1.01 V_i} = \frac{1.01 \cdot 10^5 \text{ Pa}}{1.01}$$

$$\underline{P_f^* \approx 99000 \text{ Pa}}$$

$$P_f^* + \Delta p < 1.01 \cdot 10^5 \text{ Pa}$$

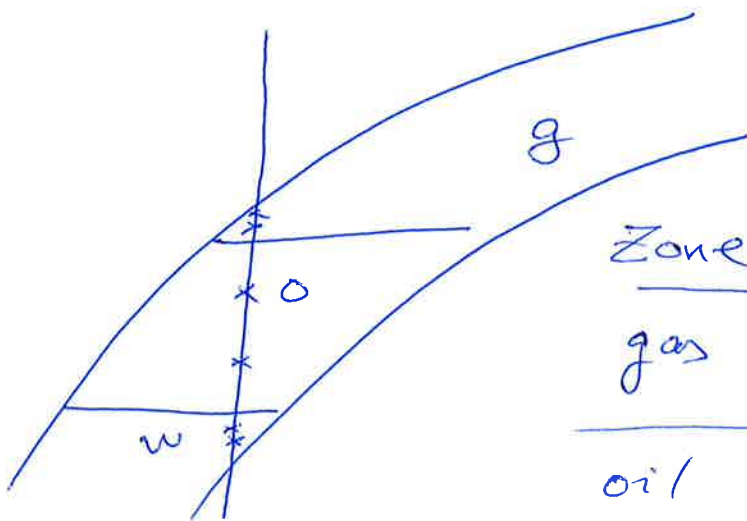




$$P_w = P_0 + \rho_w g h$$

$$P_o = P^o + \rho_o g h$$

$$P_g = P^o + \rho_g g h$$



Zone	Depth	Pressure (MPa)
gas	1865	20.07
	1915	20.17
oil	1940	20.33
	1990	20.71
water	2015	20.94
	2065	20.46

Estimate of the height of the oil zone

for each zone 2 pressures (h_a, P_a) (h_b, P_b)

linear functions $P_x = P_{ref} + \rho_x g h$

$$P_x = C_2^x + C_1^x \cdot h$$

$$\Rightarrow C_1^x = \frac{P_a - P_b}{h_a - h_b}, \quad C_2^x = P_a - h_a \cdot \frac{P_a - P_b}{h_a - h_b}$$

$$P_w = 10400h - 16 \cdot 10^3$$

$$P_o = 7600h + 5.59 \cdot 10^6$$

$$P_g = 2000h + 16.3 \cdot 10^6$$

$$\left. \begin{array}{l} \text{OWC: } P_w = P_o \Rightarrow h_{ow} = 2001 \text{ m} \\ \text{GOC: } P_o = P_g \Rightarrow h_{og} = 1920 \text{ m} \end{array} \right\} \Rightarrow \text{oil zone} \approx \underline{\underline{81 \text{ m}}}$$