

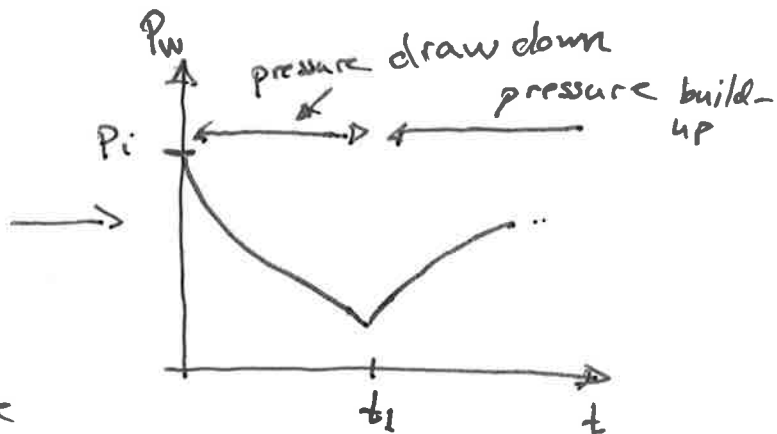
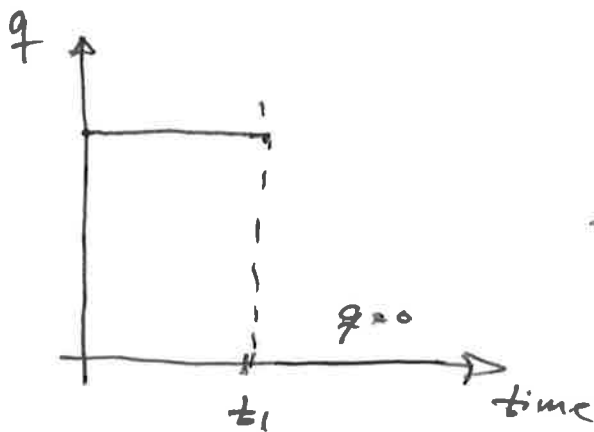
Well testing:

input: measured ~~pr~~ well pressure, flow rates, PVT-data of the fluids

1) Mathematical model that describes how the ^{reservoir} pressure change as a function of time

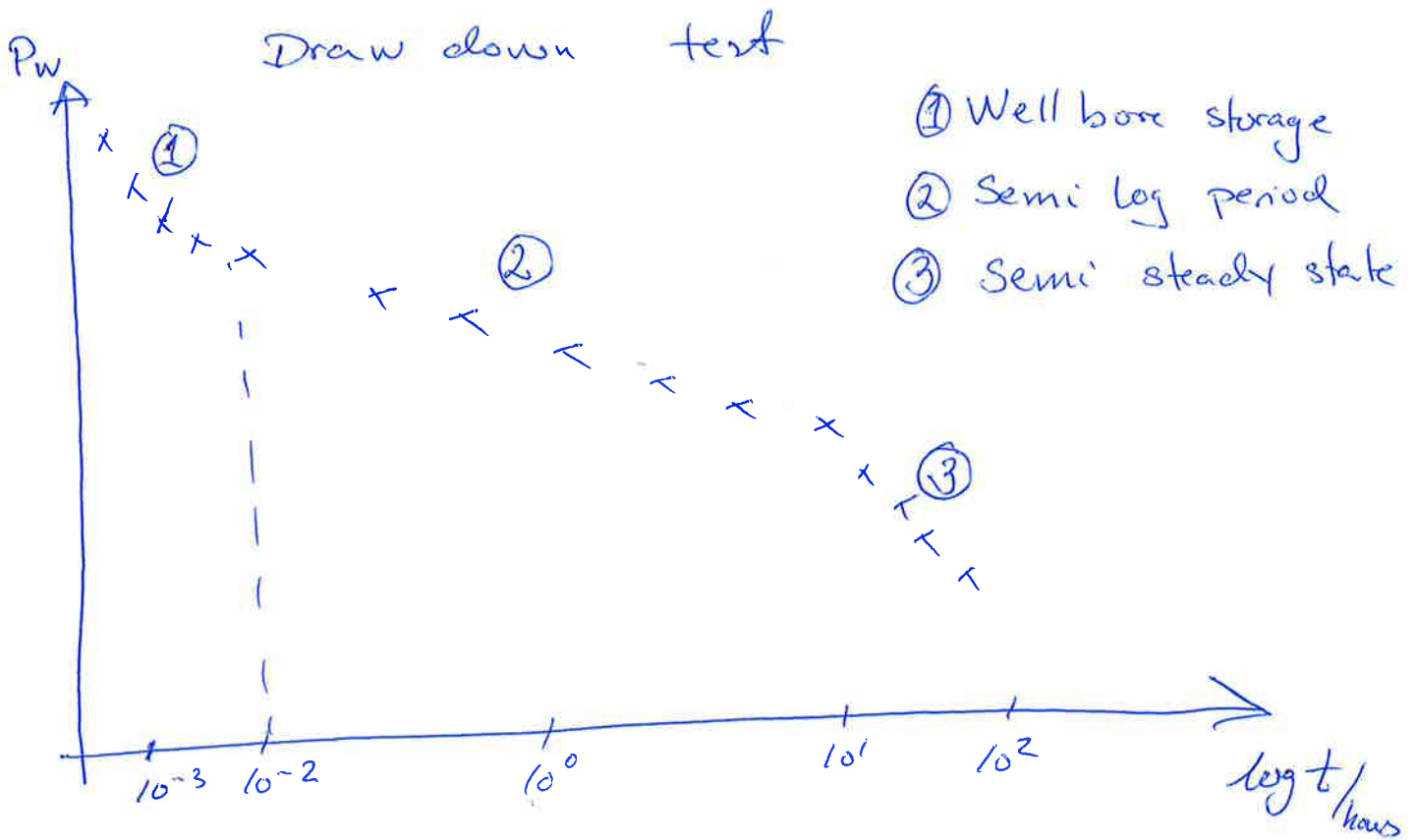
→ Diffusivity equation

2) The diffusivity equation can be solved for different boundary conditions



3) We can get information about:

- well storage capacity
- skin factor
- reservoir permeability
- drainage area (shape area)
- average reservoir pressure



① Wellbore storage



$$C_f = - \frac{1}{V_f} \frac{dV_f}{dP_f} \quad (1)$$

production $Q_f^s = \frac{\Delta V_f^s}{t} = \frac{1}{B_f} \frac{\Delta V_f}{t} \quad (2)$

assume $C_f \approx \text{constant}$

$$(1) \Rightarrow \int_{P_i}^P C_f V_f dP_f = - \int dV_f = - \Delta V_f$$

(= produced fluids)

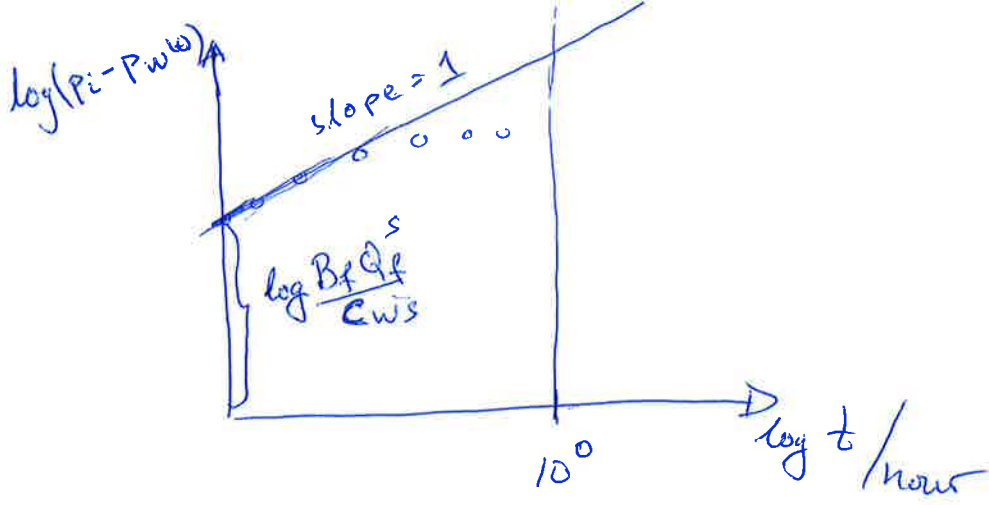
$$C_f V_f (P - P_i) = - \Delta V_f$$

$$(2) \Rightarrow Q_f^s = \frac{1}{B_f} = - \frac{1}{B_f} \frac{C_f V_f (P - P_i)}{t}$$

$$P_w(t) = P_i - \frac{B_f Q_f^s \cdot t}{V_f C_f}$$

$C_{ws} = \text{wellbore storage}$

$$\log(P_i - P_w(t)) = \log\left(\frac{B_f Q_f^s}{C_{ws}} t\right) = \log \frac{B_f Q_f^s}{C_{ws}} + \log t$$

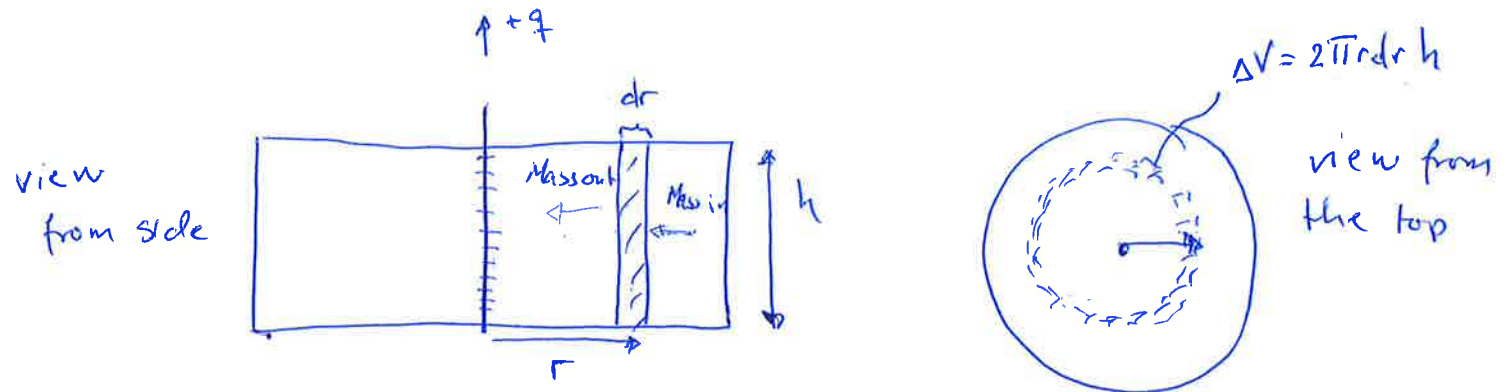


Cor

Two equations

① conservation of mass

② Darcy law



(Assumptions : homogeneous, well perforated in the whole section)

$$\textcircled{1} \quad \frac{\text{Mass in}}{\text{time}} - \frac{\text{Mass out}}{\text{time}} = \frac{\text{change in mass}}{\text{time}} \quad \overset{\sim \Delta V}{\sim}$$

$$(\rho \cdot q)_{r+dr} - (\rho \cdot q)_r = \frac{d(\rho \cdot \Delta V \cdot \varphi)}{dt}$$

$$\frac{\text{Volume}}{\text{time}} \times \frac{\text{mass}}{\text{Volume}} = \frac{\text{mass}}{\text{time}}$$

$$f(x+\Delta x) = f(x) + \frac{1}{1!} f'(x) \Delta x + \frac{1}{2!} f''(x) \Delta x^2 + \dots$$

$$\rightarrow (\rho \cdot q)_r + \frac{\partial}{\partial r} (\rho \cdot q) dr + \dots$$

$$\frac{\partial}{\partial r} (\rho \cdot q) dr = \frac{d}{dt} (\rho \cdot 2\pi r h \cdot dr \cdot \varphi)$$

$$\boxed{\frac{\partial}{\partial r} (\rho \cdot q) = 2\pi r h \frac{d}{dt} (\rho \cdot \varphi)} \quad \text{ci)}$$

② Darcy law ;

$$q = \frac{k \cdot 2\pi r h}{\mu} \frac{\partial P}{\partial r} \quad (ii)$$

(i) & (ii)

$$\Rightarrow \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial P}{\partial r} \right) = \gamma \frac{\partial P}{\partial t} \right]$$

↓ pressure
↑ pressure

$$\gamma = \frac{k}{\mu \phi C_t}$$

$C_t =$ total compressibility

$$C_t = C_p + C_f$$

\uparrow pore compressibility \uparrow fluid compressibility

$$\frac{\partial (P \cdot \phi)}{\partial t} = \phi \frac{\partial P}{\partial t} + P \frac{\partial \phi}{\partial t}$$

$$\frac{\partial \phi}{\partial t} = \frac{\partial \frac{V_p}{V_b}}{\partial t} = \frac{1}{V_b} \frac{\partial V_p}{\partial t}, \quad C_p = -\frac{1}{V_p} \frac{\partial V_p}{\partial P} \quad \leftarrow -P$$

$$\frac{\partial \phi}{\partial t} = \frac{1}{V_b} \phi C_p V_p \frac{\partial P}{\partial t} = \phi C_p \frac{\partial P}{\partial t} \quad \leftarrow \text{fluid pres.}$$

$$\frac{\partial P}{\partial t} = \frac{\partial \frac{m}{V_p}}{\partial t} = m \frac{\partial \frac{1}{V_p}}{\partial t} = -\frac{m}{V_p^2} \frac{\partial V_p}{\partial t}$$

$$C_f = -\frac{1}{V_p} \frac{\partial V_p}{\partial P} \Rightarrow \partial V_p = -C_f V_p \partial P$$

$$\frac{\partial P}{\partial t} = \frac{m C_f V_p}{V_p^2} \frac{\partial P}{\partial t} = P C_f \frac{\partial P}{\partial t}$$

$\underbrace{\hspace{10em}}_{= C_t}$

$$\rightarrow \frac{\partial}{\partial t} (P \phi) = \phi P C_p \frac{\partial P}{\partial t} + \phi P C_f \frac{\partial P}{\partial t} = \phi P (C_p + C_f) \frac{\partial P}{\partial t}$$

For diffusive processes : $D = \frac{L^2}{4t}$

For pressure : $\eta = \frac{L^2}{4t}$

$\eta \approx k = 1 D \approx 1 (\mu\text{m})^2 = 10^{-12} \text{ m}^2$

$\mu = 1 \text{ cP} = 10^{-3} \text{ Pa} \cdot \text{s}$

$C_t = 10^{-5} / \text{psi} \approx 1.45 \cdot 10^{-9} \text{ 1/Pa}$

$\varphi \approx 0.3$

$\eta = \frac{10^{-12} \text{ m}^2}{10^{-3} \text{ Pa} \cdot \text{s} \cdot 0.3 \cdot 1.45 \cdot 10^{-9} \text{ 1/Pa}} \approx \underline{\underline{23 \text{ m}^2/\text{s}}}$

$L = 7 \text{ cm} = 7 \cdot 10^{-2} \text{ m}$

$t = \frac{L^2}{4D} = \frac{(7 \cdot 10^{-2} \text{ m})^2}{4 \cdot 2.3 \text{ m}^2/\text{s}} = \underline{\underline{5.3 \cdot 10^{-4} \text{ s}}}$

$L = 1 \text{ km} \Rightarrow t = \frac{(10^3 \text{ m})^2}{4 \cdot 2.3 \text{ m}^2/\text{s}} = 1.087 \cdot 10^5 \text{ s} \approx \underline{\underline{30 \text{ hours}}}$