## PET565 PART B: EXERCISE SET 2

## Goals

- Use thermodynamics theory to predict equilibrium constants.
- Become familiar with carbon chemistry and relevant reactions.
- Be familiar with the concept of ion exchange and basic definitions.
- Perform simple calculations on equilibrium compositions

## IMPORTANT NOTES

- The activity of a gas species is given by its partial pressure. At atmospheric conditions the partial pressure in magnitude of atmospheres (as if the unit was atmospheres) corresponds to the activity. Typically  $CO_2$  has partial pressure of  $10^{-3.5}$ atm.
- In an open system (between a brine and atmosphere) the brine is in equilibrium with the atmosphere (given sufficient time).
- In a closed system (only involving a brine) the total inorganic carbon, TIC, is constant.
- pH is defined as  $pH = -\log([H^+])$

# 1. Exercises

- **1.1.** Show by integration that van't Hoffs equation (4.28) results in equation (4.29). Which assumptions are made?
- 1.2. Villiaumite, NaF (s) is a mineral that dissolves according to

$$NaF(s) \rightarrow Na^{+}(aq) + F^{-}(aq)$$
 (1)

The following table values (measured at 25 C) are given:

$$\Delta G_{f,NaF}^0 = -543.5, \quad \Delta G_{f,Na^+}^0 = -261.9, \quad \Delta G_{f,F^-}^0 = -278.8 \quad (kJ/mol),$$
 (2)

$$\Delta H_{f,NaF}^0 = -573.6$$
,  $\Delta H_{f,Na^+}^0 = -240.1$ ,  $\Delta H_{f,F^-}^0 = -332.6$  (kJ/mol), (3)

and  $R = 8.314 \cdot 10^{-3} \text{kJ/mol/deg}$ .

- Calculate  $\Delta G_r^0$  and  $\Delta H_r^0$  for the reaction above.
- Calculate the solubility constant of villiaumite at 25C using equation (4.26).
- Use Van't Hoffs equation (4.29) to calculate the solubility constant at 10C.
- **1.3.** We here consider the role of carbon species on pH in a brine.

The following reactions represent the interaction between water and carbon in a system OPEN to the atmosphere:

$$CO_2(g) + H_2O(g) \rightarrow H_2CO_3^*(aq)$$
 (4)

$$H_2CO_3^*(aq) \rightarrow H^+(aq) + HCO_3^-(aq)$$
 (5)

$$HCO_3^-(aq) \rightarrow H^+(aq) + CO_3^{2-}(aq)$$
 (6)

$$H_2O(aq) \rightarrow H^+(aq) + OH^-(aq)$$
 (7)

where the equilibrium constants are respectively  $K_H = 10^{-1.5}, K_1 = 10^{-6.3}, K_2 = 10^{-10.3}, K_w = 10^{-14}$ .

- For reference, if carbon is not available, only the fourth reaction is relevant. Calculate the pH in this case.
- Now assume carbon can enter the brine from the atmosphere. Express equilibrium equations for the 4 above reactions. Assume a dilute brine (i.e.  $\gamma = 1$ ).
- List the 6 independent variables of the system.

• Assume  $P_{co2}$  and pH are known parameters (determined by atmosphere composition and brine composition, respectively).

Solve the system and determine the concentrations of aqueous carbon species:  $m_{\rm H_2CO_3^*}$ ,  $m_{\rm HCO_3^-}$  and  $m_{\rm CO_3^-}$  as function of  $P_{co2}$  and pH.

PS: Note that  $m_{oh}$  follows directly from pH and does not require calculation.

- Calculate the TIC as a function of  $m_{\mathrm{H}^+}$  and  $P_{co2}$ .
  - What is the effect of  $P_{co2}$  on TIC?
  - What is the effect of pH (as given by  $m_{\rm H^+}$ ) on TIC?
  - Which species become more dominating (has higher fraction of the TIC) at different pH?
- Assume now that the pH is unknown and only the listed species above are in the brine.
  - Formulate the charge balance equation for the brine species:

$$\sum_{i} m_i z_i = 0 \tag{8}$$

- Simplify this equation by assuming an acidic solution. Then  $m_{co3}$  can be ignored. Insert the expressions of  $m_{hco3}$  and  $m_{oh}$  as function of  $m_h$ . Solve with respect to  $m_h$
- Use that  $P_{co2} = 10^{-3.5}$  (typical atmospheric value) and calculate the pH. This is the pH due to carbon entering distilled water. Compare with the first task.

## 1.4.

- A sample of 100g (dry weight) quartz rock stores on its surface 0.5mmol Na<sup>+</sup>, 1.0mmol Ca<sup>2+</sup> and 0.5mmol Mg<sup>2+</sup>. Calculate the cation exchange capacity, CEC in terms of mmeq/kg rock.
- The rock has grain density 2.65g/cc and porosity 0.3. Calculate the CEC in terms of mmeq/l pore volume.
- 1.5. Find the equilibrium constant K for ion exchange of  $Mg^{2+}$  and  $Ca^{2+}$  corresponding to the reaction of the form

$$\operatorname{CaX}_2 + \operatorname{Mg}^{2+}(aq) \rightarrow \operatorname{MgX}_2 + \operatorname{Ca}^{2+}(aq)$$
 (9)

Use the theory from pages 254-255 and the reference reactions with Na<sup>+</sup> to derive the correct result.