

# Exam V14

## Problem 1

a) Calculate pore pressure at the top of the reservoir

$$P_{@ \text{OWC}} = S_w \rho g h_w = 1,03 \cdot 0,0981 \cdot 1050 = \underline{106 \text{ bar}}$$

$$P_{@ 520 \text{ m}} = \underline{52 \text{ bar}} \text{ (outside res.)}$$

$$\begin{aligned} P_{@ 520 \text{ m}} &= 106 \text{ bar} - S_o \rho g h_o - S_g \rho g h_g \\ &= 106 \text{ bar} - 0,15 \cdot 0,0981 \cdot (860 - 520) \\ &\quad - 0,83 \cdot 0,0981 \cdot (1050 - 860) \\ &= 106 \text{ bar} - 5 \text{ bar} - 15,5 \text{ bar} \\ &= \underline{85,5 \text{ bar}} \text{ (inside res.)} \end{aligned}$$

If you are asking for the pressure outside the reservoir, the pressure is 52 bar. Inside the reservoir, the pressure is 85,5 bar

Wu We need hydrostatic pressure of mud to be 91,5 bar.

$$P = S_m \rho g h \Rightarrow S_m = \frac{91,5}{0,0981 \cdot (520 + 24)}$$

riser air gap

$$\rho_m \sim 1,715 \text{ s.g}$$

Note that if riser has to be disconnected due to stormy weather, the mud weight must be increased to include riser margin, but 1.715 s.g is the minimum mud weight

b) Reservoir DWC extends down to 1300m

$$P@520(\text{inside}) = \rho_w g h_w - \rho_o g h_o - \rho_g g h_g$$

$$85,5 = \rho_w g h_w - \rho_o g (1300 - h) - \rho_g g (h - 520)$$

$$85,5 = 131,4 - \rho_o g 1300 + \rho_o g h - \rho_g g h + \rho_g g 520$$

$$= 131,4 + h(\rho_o - \rho_g)g + g(\rho_g 520 - \rho_o 1300)$$

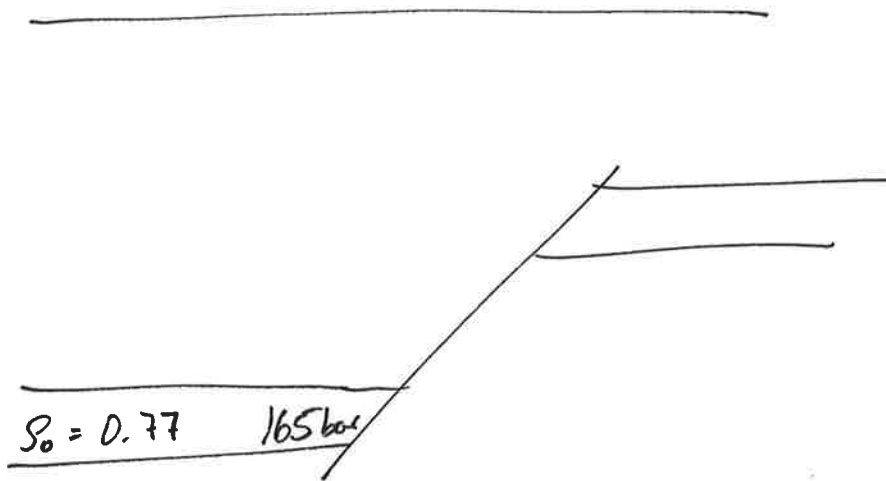
$$\frac{85,5 - 131,4 - g(\rho_g 520 - \rho_o 1300)}{(\rho_o - \rho_g)g} = h$$

$$h = \frac{85,5 - 131,4 - 0,0981(0,15 \cdot 520 - 0,83 \cdot 1300)}{(0,83 - 0,15) \cdot 0,0981} = \underline{\underline{787,1}}$$

Assuming no overpressure

$$\text{with } 1,715 \text{ s.g} \Rightarrow \underline{h = 874}$$

C)



i) open fault :

Pressure at B1

$$165 \text{ bar} - \rho_0 g h_0$$

$$165 \text{ bar} - 0.77 \cdot 0.0981 \cdot (1250 - 860)$$

$$165 \text{ bar} - 29,5 \text{ bar}$$

$$\underline{135,5 \text{ bar}}$$

ii) Same pressure : 165 bar

d) Mud weight , 5 bar overpressure

$$B1, \text{ open fault : } P = \rho_m g h \Rightarrow \rho_m = 1,66 \text{ s.g}$$

$\rho_m = 2,01$  : closed fault

## Problem 2

a) Compute the burst strength

$$P110 \Rightarrow \text{yield} = 110 \text{ kpsi} \\ = \underline{\underline{7483 \text{ bar}}}$$

$$P_{\text{burst}} = 2 \sigma_{\text{tensile}} \left( \frac{t}{D_o} \right)$$

$$t = \frac{508 - 475,7}{2} = \underline{16,15}$$

$$= 2 \cdot 7483 \cdot \frac{16,15}{508} = \underline{\underline{475,8 \text{ bar}}}$$

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$$K55 \Rightarrow \sigma = 55000 \text{ psi} = \underline{\underline{3741,5 \text{ bar}}}$$

$$P_{\text{burst}} = 2 \sigma_{\text{tensile}} \left( \frac{t}{D_o} \right)$$

$$= 2 \cdot 3741,5 \cdot \left[ \frac{(346,1 - 314,3)/2}{346,1} \right] = \underline{\underline{343,7 \text{ bar}}}$$

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$$N80 \Rightarrow \sigma = 80000 \text{ psi} = \underline{\underline{5442 \text{ bar}}}$$

$$P_{\text{burst}} = 2 \cdot 5442 \cdot \left[ \frac{(273 - 245,4)/2}{273} \right] = \underline{\underline{550 \text{ bar}}}$$

L80

$$P_{burst} = 2 \cdot 5442 \cdot \frac{(177.8 - 164)2}{177.8} = \underline{\underline{422.4 \text{ bar}}}$$

From strongest to weakest

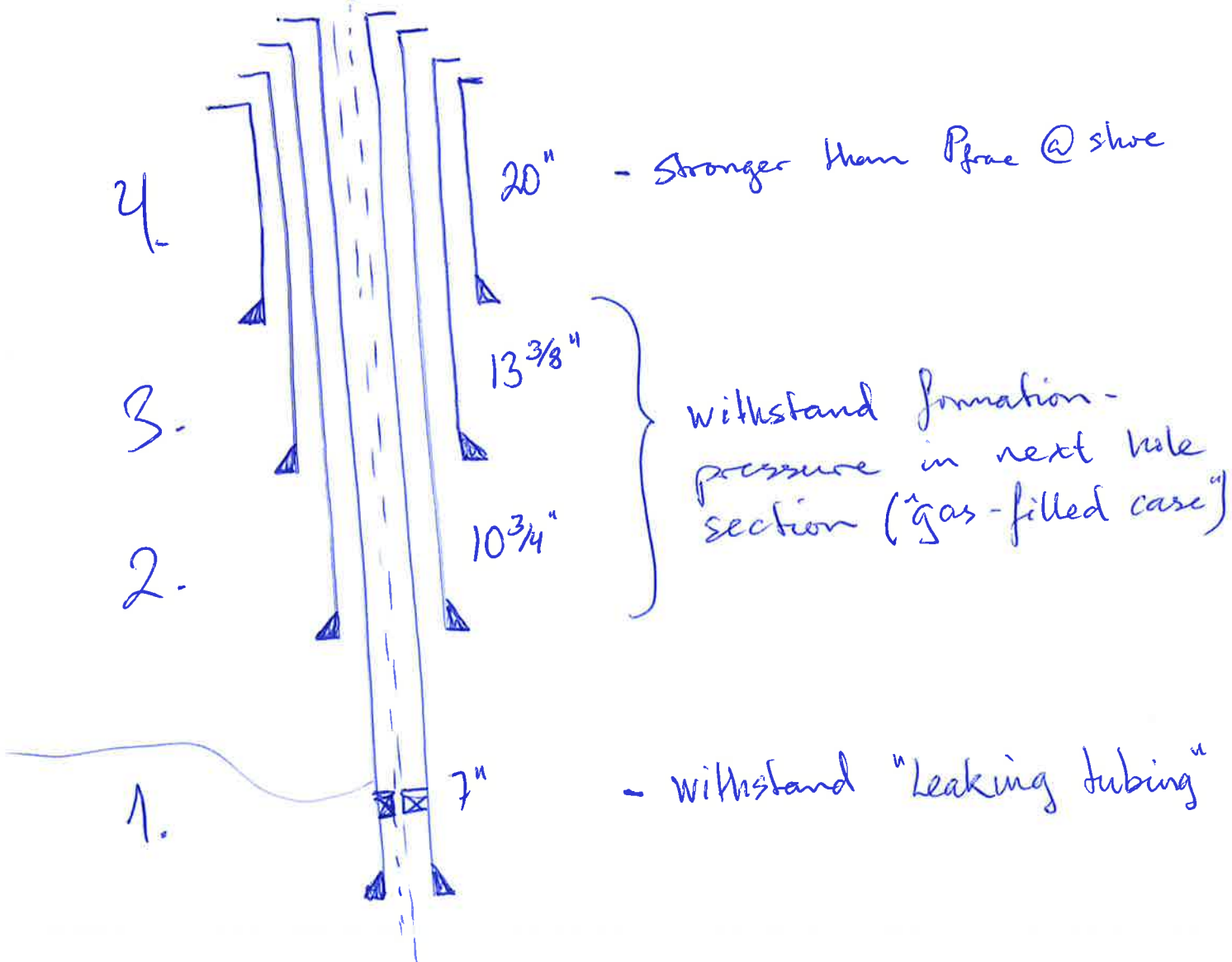
N80 - 10  $\frac{3}{4}$  - 550

P110 - 20 - 475

L80 - 7 - 422  $\Rightarrow$  increase strength

K55 - 13  $\frac{3}{8}$  - 343  $\Rightarrow$  increase strength

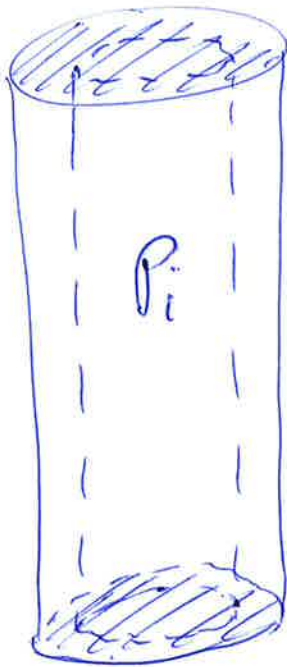
b) Suitable for use in the same well?



# C) Pressurized closed pipe

Pressurized from inside

$$P_i \gg P_o$$



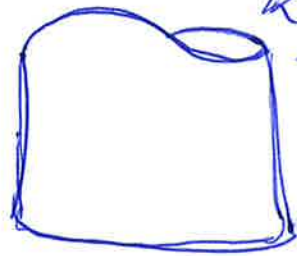
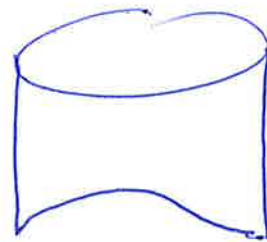
$P_o$

Case 1: burst

Case 2: Axial

Case 1:

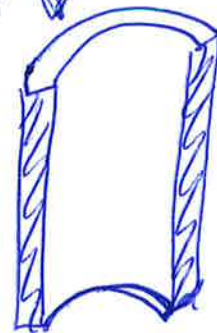
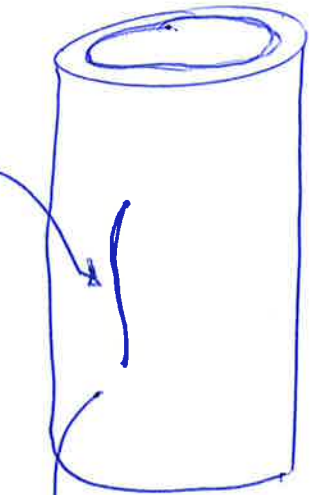
Case 2:



A:



A:

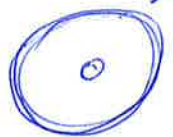


(Assuming inside pressure at 400 bar)

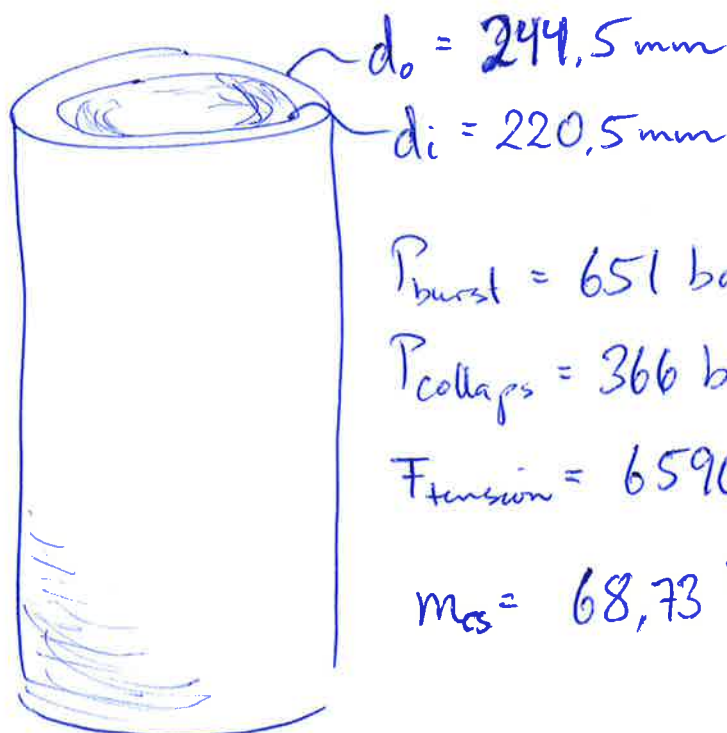
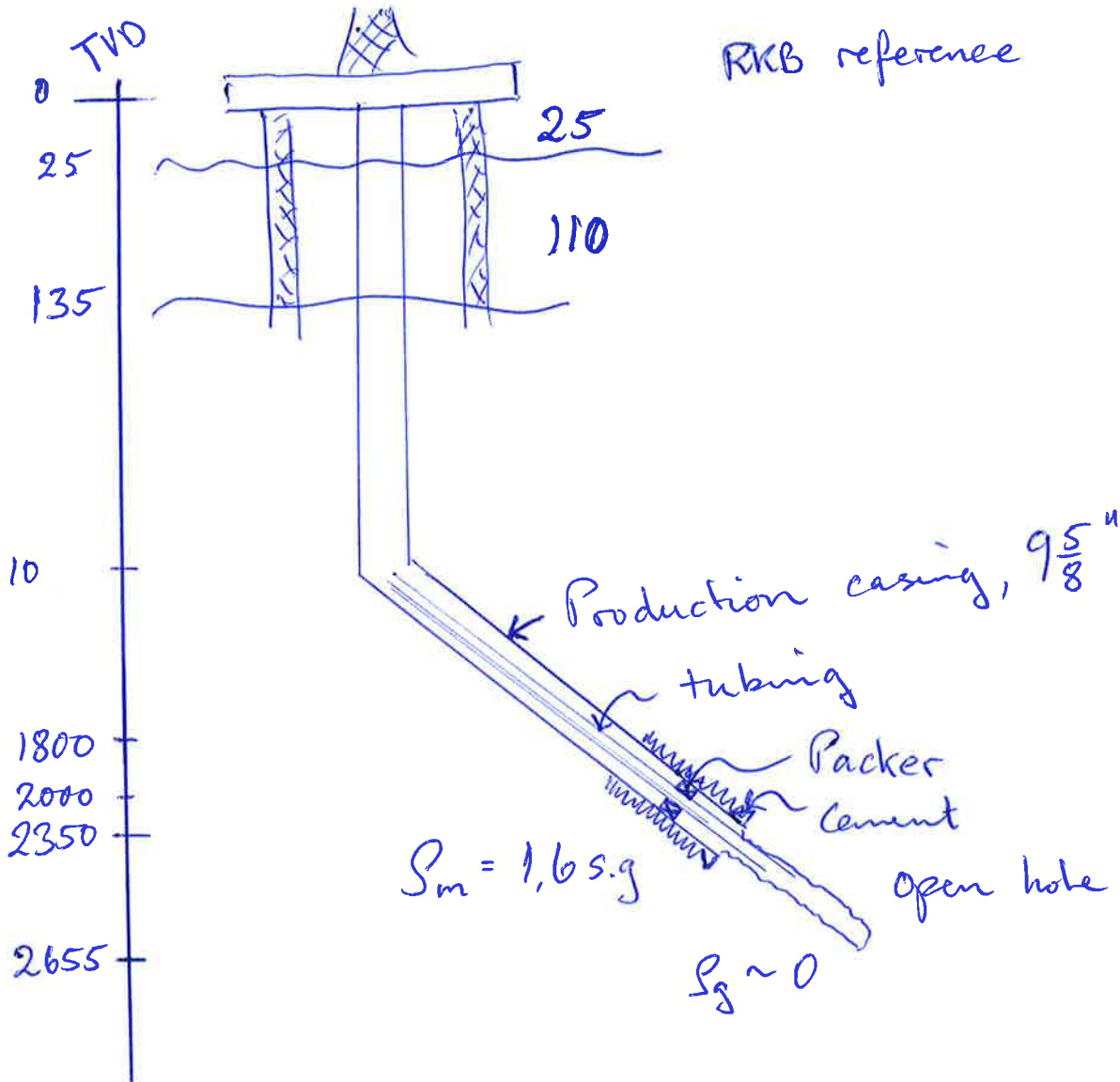
$$P_{burst} = 2\sigma_{tensile} \frac{t}{D_o}$$

$$P_{tear} = \sigma_{tensile}$$

$$t \geq \frac{D_o}{2}$$



# Problem 3



$P_{burst} = 651 \text{ bar}$

$P_{collapse} = 366 \text{ bar}$

$F_{tension} = 6590 \text{ kN}$

$m_{cs} = 68.73 \text{ kg/m}$

## a) Criteria for burst

- Production casing

- Gas-filled casing
- Leaking tubing

- Gas-filled casing:

- At wellhead

~~P<sub>i</sub>~~  $P_i = \text{BHP} - \cancel{S_g g h_g} = \text{BHP} = 15 \cdot 0.098 \cdot 2350$  fig 1.  
↓

$P_o = 0$  ↑  
highest pore  
pressure

$\Delta P = 345,8 \text{ bar}$

- At casing shoe

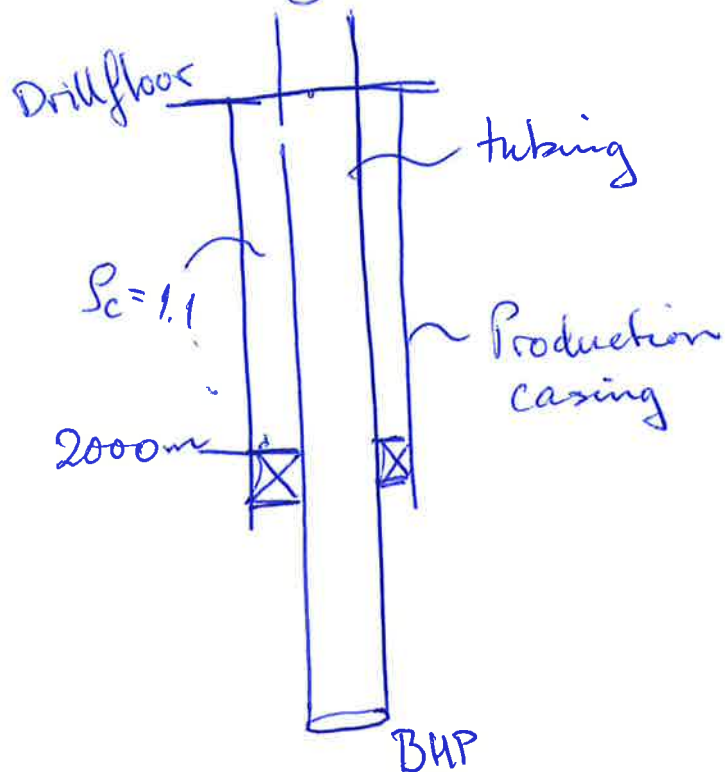
$$P_i = 345,8 \text{ bar}$$

$$P_o = S_w g h_w = 1,03 \cdot 0,0981 \cdot (2350 - 25)$$
$$= 235 \text{ bar}$$

$\Delta P = 110 \text{ bar}$



- Leaking tubing



$$\begin{aligned}
 P_i = P_{@ \text{Packer}} &= \text{BHP} + S_c g h_c \\
 &= 345,8 + 1,1 \cdot 0,0981 \cdot 2000 \\
 &= \underline{561,6 \text{ bar}}
 \end{aligned}$$

$$\begin{aligned}
 P_o = S_w g h_w &= 1,03 \cdot 0,0981 \cdot (2000 - 25) \\
 &= \underline{200 \text{ bar}}
 \end{aligned}$$

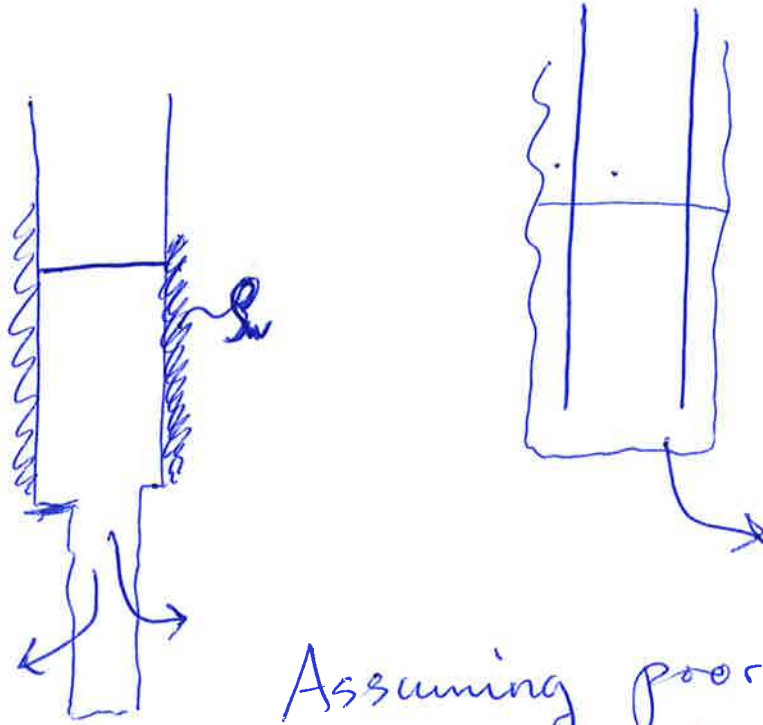
$$\underline{\Delta P = 362 \text{ bar}}$$

$$\text{DF} = \frac{651}{362} = \underline{\underline{1,8}} \Rightarrow \text{ok}$$

above 1.18 is recommended.

# Collapse

- loss to thief zone



Assuming poor cement job  $\Rightarrow$   $S_m$  outside casing

$$Frac @ 2350 = 1,615,000 \text{ s.g}$$

$$\begin{aligned}
 P_{frac} &= 4.6 \cdot 0.0981 \cdot 2350 \cdot 1.03 \\
 &= 1.03 \cdot 1.62 \cdot 0.0981 \cdot (2350 - 25) \\
 &= \underline{\underline{1352}} = 231.9
 \end{aligned}$$

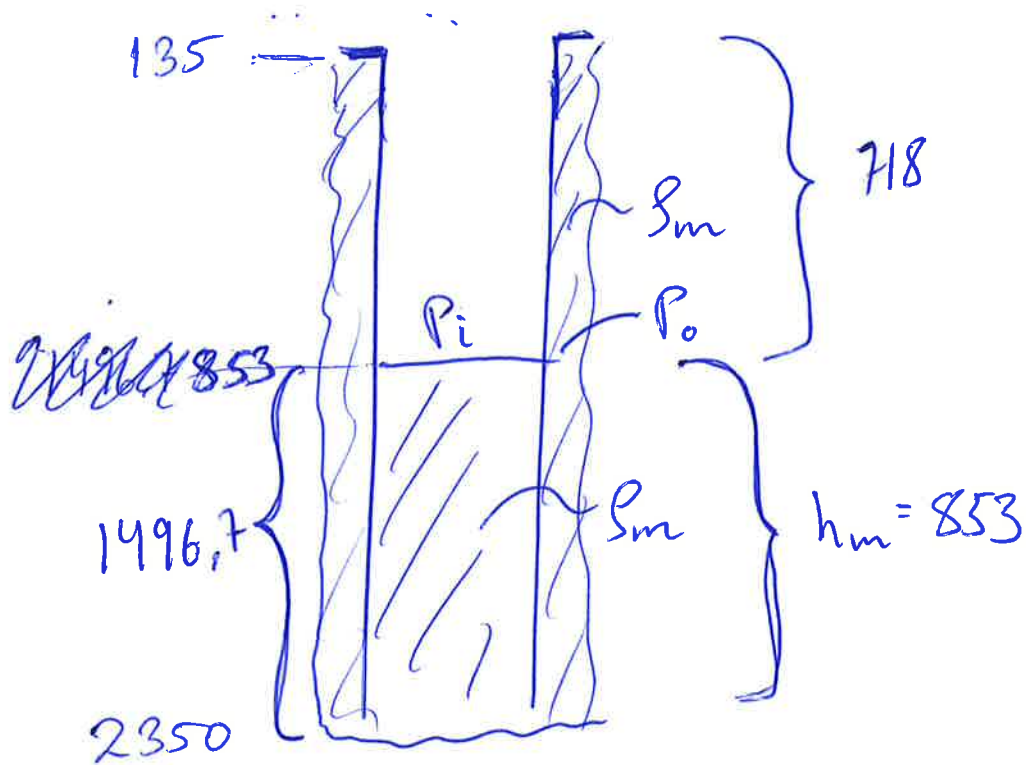
Mud in casing must balance frac. pressure.

$$\begin{aligned}
 395 &= S_m g h_{mud} \Rightarrow h = \frac{395}{0.098 \cdot 1.03} = \underline{\underline{2203 \text{ m}}} \\
 h &= 1496.7
 \end{aligned}$$

$$P_i = 0$$

$$P_o = \rho_m g h_m + \rho_w g h_w$$

$$= 1,6 \cdot 0,0981 \cdot (2350 -$$



~~1496,7~~

$$P_o = \rho_m g h_m + \rho_w g h_w$$

$$= 1,6 \cdot 0,0981 \cdot 718 = \underline{112 \text{ bar}}$$

$$112 + 11 = 123$$

$$\Delta P = 123 \text{ bar}$$

$$DF = \frac{366}{123} = 3 \Rightarrow \text{ok}$$

C) Weight in air

$$mes \cdot 9,81 \cdot 2909$$

$$68,73 \cdot 9,81 \cdot 2909 = \underline{1961,4 \text{ kN}}$$

Bouyed weight

$$\left(1 - \frac{\rho_m}{\rho_s}\right) \cdot W = 1961,4 \cdot \left(1 - \frac{1,6}{7,85}\right)$$

$$= 1561,6 \text{ kN}$$

$$DF = \frac{6590}{1821} = \underline{3,6}$$

$$DF = \frac{6590}{1561} = 4,2 \Rightarrow \text{OK}$$

Pressure test, assume wellhead to handle 10000 psi = 680 bar

$$A = \frac{\pi}{4} d_i^2$$

$$= \frac{\pi}{4} \cdot (220,5 \cdot 10^{-3})^2$$

$$= 3820 \text{ cm}^2$$

$$\% T = 23,6\%$$

$$\% C = -87\%$$

$$P = \frac{F}{A}$$

$$F = PA$$

$$= 680 \cdot 3,82$$

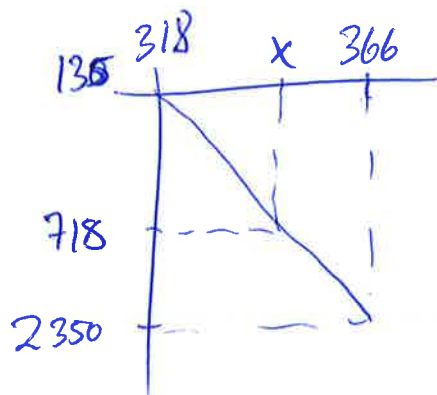
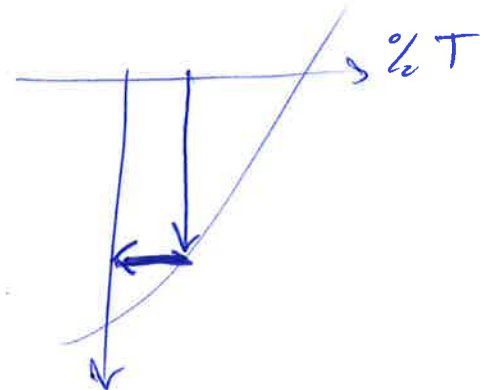
$$= 2596 \text{ daN}$$

$$= 259,6 \text{ kN}$$

$$P_{\text{collaps, new at } t_p} = \underline{318} \text{ \% C}$$

$$P_{\text{collaps}} = 366$$

$$P_{\text{collaps @ 718}}$$



$$\frac{366 - 318}{2350 - 135} = \frac{x - 318}{718 - 135}$$

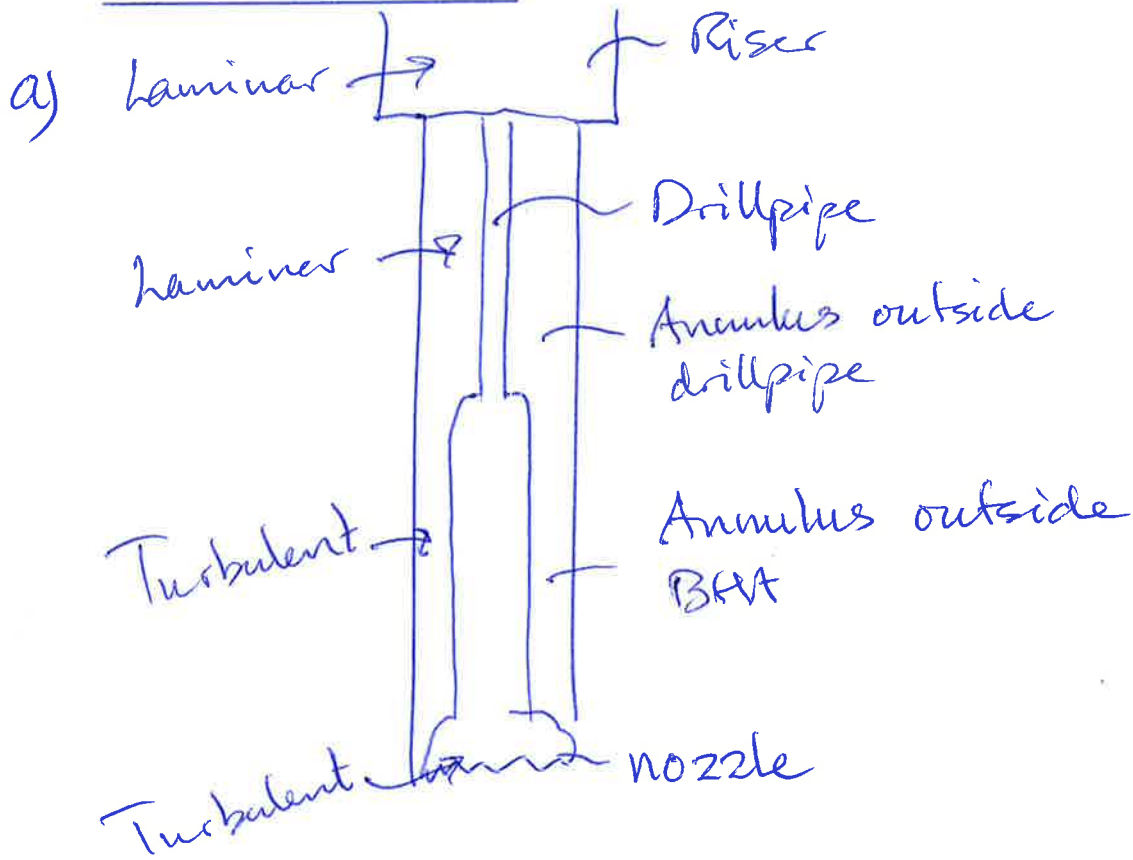
$$x = 318 + \frac{366 - 318}{2350 - 135} (718 - 135)$$

$$\underline{x = 330}$$

$$P_{\text{collapse}} = \underline{330}$$

$$DF = \frac{330}{123} = \underline{\underline{2.69}}$$

# Problem 4



Most of the length of the well is drillpipe  
 $\Rightarrow$  laminar flow is most common.

b) Pressure drop

laminar :  $P \sim \mu q$

Turbulent :  $P \sim S q^2$

$$\frac{S \cdot V D}{\mu} \frac{16}{\pi}$$

~~viscosity, friction against flow~~

Most of the  $\Delta P$  in nozzle and annulus outside BHA

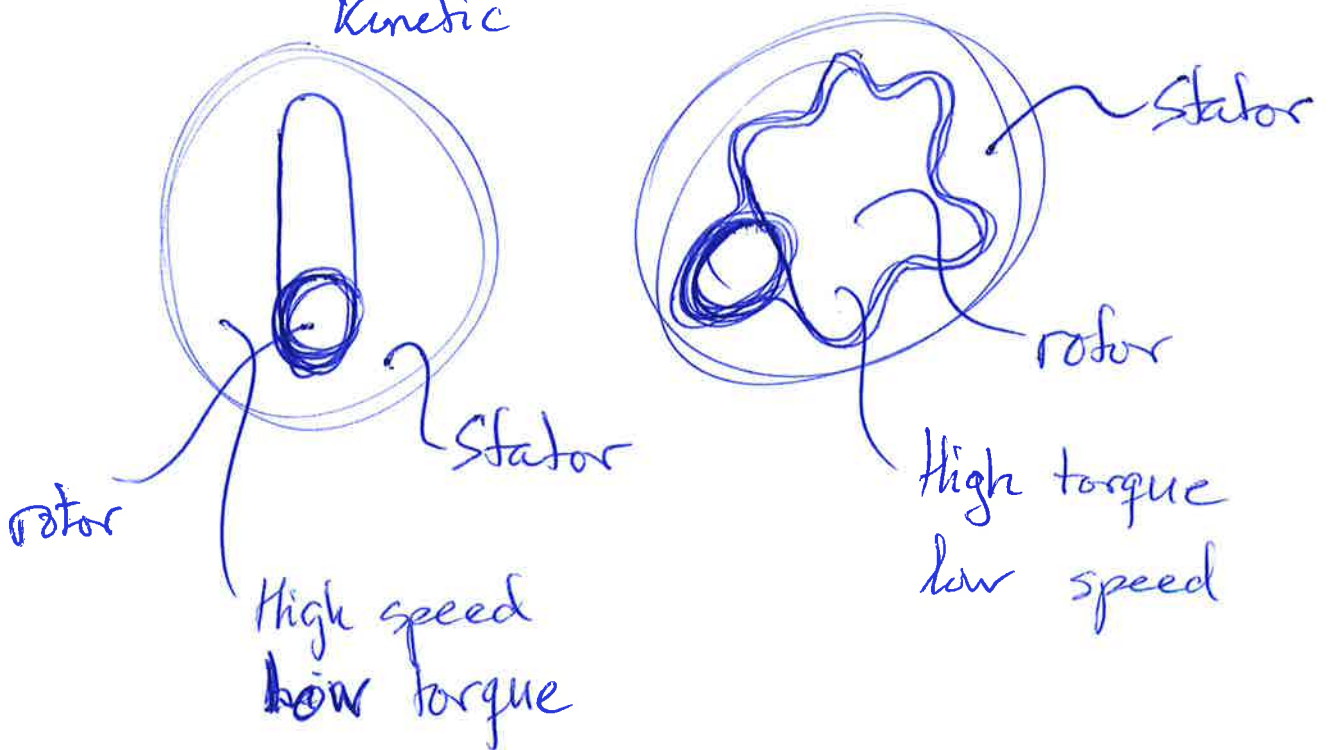
$\Rightarrow S$  is dominating

$$P_2 = \frac{S q^2}{2A^2 0.95^2}$$

## c) RSS vs motor

There is a large pressure drop through the motor in order to turn the drillbit

⇒ hydraulic energy is converted to ~~mechanical~~ kinetic energy.



d)  $3,5'' \rightarrow 5''$  assuming that ID increases

Three improvements

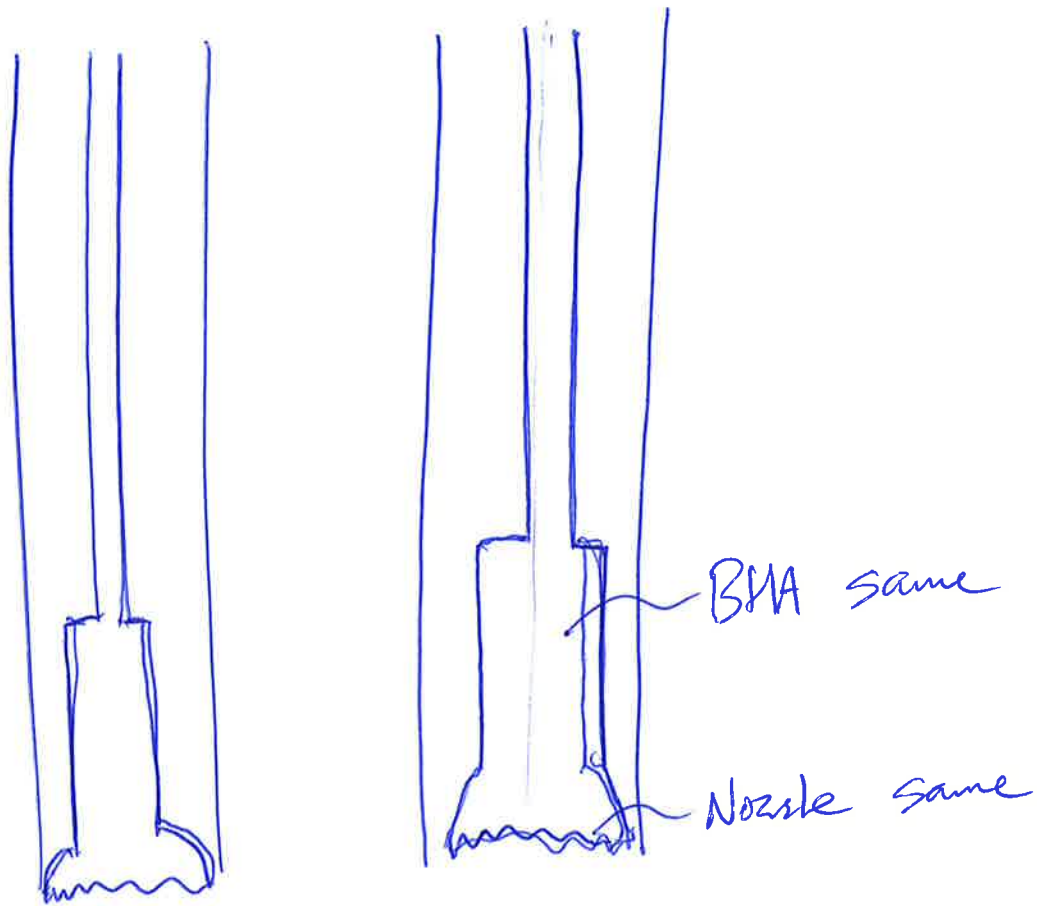
$P_1$  = Pump pressure

$P_2$  = Pressure loss through nozzle

$P_3$  = parasitic pressure loss

3.5

5"



5"  $\Rightarrow$  ~~more~~ less parasitic pressure loss inside drill pipe

$$P_1 = P_2 + P_3 \quad ; \quad P_3 \text{ unchanged}$$

$P_1 \rightarrow$  lower

$\hookrightarrow$  increased pump capacity

$\hookrightarrow$  same hydraulic effect through nozzle with lower pump pressure



## e) Mechanical power

$$T_2 = \dot{m}v = \rho qv$$

mass rate                      density                      fluid velocity                      flow rate

## Hydraulic power

$$HP = P_2 q$$

Pressure drop through nozzle                      flow rate

# Problem 5

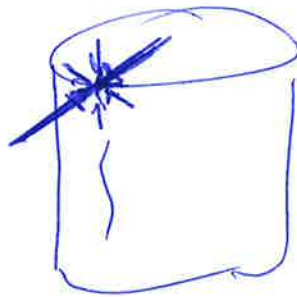
a) limits for mud weight

- Pore pressure / collapse pressure
- Fracture pressure / LOT

Failure mechanisms

- Tensile

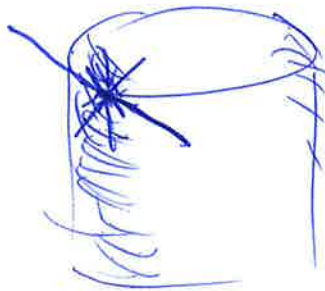
↳ too high mud weight



$$\sigma_{\theta} = 2\sigma_a - P_w$$

- Tangential / Hoop stress

↳ too low mud weight  $\Rightarrow$  collapse



## b) Fracture equation

Simplest equation

$$P_{wf} = \sigma_a \quad \text{No filter cake}$$

$$P_{wf} = 2\sigma_a - P_o \quad \text{filter cake}$$

$$\sigma_a = \frac{1}{2}(P_{wf} - P_o) \quad ; P_o = \text{pore pressure}$$

⇒ Keep the mud weight equal to the in-situ stress

~~i.e.~~ between the fracture pressure and the pore pressure

This is called "the median line principle"

## c) Advantages

- No change in the stress state in the rock.

